

CCEA A2 Mathematics & Further Mathematics

Teaching Schedules

Updated August 2020

These schedules are based upon shared teaching with equal times for each of 2 teachers.

Please note that this teaching order should be followed by all teachers.

They will allow either **consecutive or parallel teaching** of A2 Mathematics and Further Mathematics.

Mathematics

This schedule is designed to cover **all of Unit 1 first**, then followed by Unit 2A and Unit 2B.

Further Mathematics

These schedules are designed to cover **all of Unit 1 first**, then followed by each of the other two Applied units.

A2 Mathematics

Week	Teacher 1	Teacher 2
1	Partial Fractions <ul style="list-style-type: none"> Simplify rational expressions by factorising, cancelling and algebraic division Decompose rational functions into partial fractions 	Trigonometry <ul style="list-style-type: none"> Radian measure Arc length and sector area Definitions of secant, cosecant, cotangent Definitions of arcsin, arccos and arctan Graphs of each function, including domains and ranges Use of <ul style="list-style-type: none"> $\sec^2 \theta = 1 + \tan^2 \theta$ $\operatorname{cosec}^2 \theta = 1 + \cot^2 \theta$ Compound angle formulae for sine, cosine and tangent Double angle formulae Harmonic form Construct proofs involving trig functions and identities Use of trig functions to solve problems in context
2	Differentiation (i) <ul style="list-style-type: none"> Differentiation of exponential, logarithmic and trig functions and their related sums, differences and constant multiples Chain rule Product rule Quotient rule 	
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6	Integration <ul style="list-style-type: none"> Integrate e^{kx}, $\frac{1}{x}$, $\sin kx$, $\cos kx$ and related functions Area between 2 curves Integration using <ul style="list-style-type: none"> Substitution Parts Partial fractions Volumes of revolution 	
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10	Parametric Equations <ul style="list-style-type: none"> Use parametric equations of curves Convert between parametric and Cartesian forms 	
11	Differentiation(ii) <ul style="list-style-type: none"> Differentiation of simple functions defined implicitly or parametrically To include second derivatives 	
12	Differential Equations <ul style="list-style-type: none"> Construct and solve simple differential equations Interpret solution and identify limitations 	
13		
14	Numerical Methods <ul style="list-style-type: none"> Use of trapezium rule as an approximation to the area under a curve Location of roots Newton-Raphson method 	Binomial <ul style="list-style-type: none"> Expansion of $(a + bx)^n$ for any rational n Knowledge of range of validity
15		Functions <ul style="list-style-type: none"> Definition and terminology Composite function Inverse functions and graphs Modulus function
16	Moments <ul style="list-style-type: none"> Use moments in simple static contexts – to include <ul style="list-style-type: none"> Rods Ladders Hinged beams 	Graph Transformations Combination of simple transformations
17		Kinematics and calculus <ul style="list-style-type: none"> Motion in a straight line Motion in two dimensions in vector form
18		
19		

Week	Teacher 1	Teacher 2
20	Impulse and Momentum <ul style="list-style-type: none"> • Simple use of impulse and momentum • Conservation of linear momentum • Problems to involve direct collisions and explosions 	Projectiles <ul style="list-style-type: none"> • Solve problems involving projectiles – may include vector format • Derive and use formulae for time of flight, range, equation of path of flight
21		
22	Normal distribution <ul style="list-style-type: none"> • Use of the normal distribution as an example of a continuous probability distribution • Find probabilities using the normal distribution • Selection of an appropriate binomial/normal model for a specific context 	Hypothesis Testing <ul style="list-style-type: none"> • Understand and use the language of hypothesis testing • Conduct a hypothesis test for <ul style="list-style-type: none"> ○ the proportion in the binomial distribution ○ the mean of a normal distribution • Interpret results of hypothesis test in context
23		
24	Probability <ul style="list-style-type: none"> • Use of conditional probability – to include tree diagrams, Venn diagram and two-way tables • Use of the conditional probability formula • Solution of problems in context 	
25		
26	Hypothesis Testing <ul style="list-style-type: none"> • Interpret a correlation coefficient using a p-value or critical value 	

A2 Further Mathematics Units 1, 2A & 2B

Week	Teacher 1	Teacher 2
1	<p><u>Further Circular Motion¹</u></p> <ul style="list-style-type: none"> Banked corners Sliding Overturning (some introductory work on Moments will be required) 	<p><u>Polar Coordinates</u></p> <ul style="list-style-type: none"> Convert between polar and Cartesian coordinates Sketch curves with r given as function of θ Area enclosed by a polar curve
2		
3		
4	<p><u>Induction</u></p> <ul style="list-style-type: none"> Construction of proofs involving e.g. <ul style="list-style-type: none"> Sums of series Divisibility Powers of matrices 	<p><u>Complex numbers</u></p> <ul style="list-style-type: none"> Use of De Moivre's Theorem to find <ul style="list-style-type: none"> Multiple angle formulae Sums of series Use of <ul style="list-style-type: none"> $e^{i\theta} = \cos \theta + i \sin \theta$ $z = re^{i\theta}$ Find nth roots of $re^{i\theta}$ and relate to Argand diagram Use complex roots of unity to solve geometric problems
5		
6		
7	<p><u>Hyperbolic Functions</u></p> <ul style="list-style-type: none"> Definitions of $\sinh x$, $\cosh x$ and $\tanh x$, including domains, ranges and graphs Differentiate hyperbolic functions Integrate hyperbolic functions Definitions of inverse hyperbolic functions, including domains and ranges Derive and use the logarithmic forms of the inverse hyperbolic functions 	<p><u>Simple Harmonic Motion²</u></p> <ul style="list-style-type: none"> Standard results Solution of SHM equation Simple pendulum Oscillations involving elastic strings
8		
9		
10	<p><u>Further Calculus</u></p> <ul style="list-style-type: none"> Evaluate improper integrals Integration using partial fractions – to include quadratic factors in denominator Differentiate inverse trig functions Integrate functions of the form $(a^2 - x^2)^{-1/2}$ and $(a^2 + x^2)^{-1}$ and choose the appropriate trigonometric substitutions to integrate associated functions Integrate functions of the form $(x^2 + a^2)^{-1/2}$ and $(x^2 - a^2)^{-1/2}$ and choose the appropriate hyperbolic substitutions to integrate associated functions Repeated integration by parts Reduction formulae 	<p><u>Series</u></p> <ul style="list-style-type: none"> Decompose rational functions into partial fractions – to include quadratic factors in denominator Use of formulae for sums of integers, squares and cubes to find sums of other series Use method of differenced for summation of series – to include use of partial fractions Find the Maclaurin series of a function – to include the general term Recognise and use the Maclaurin series for e^x, $\ln(1 + x)$, $\sin x$, $\cos x$ and $(1 + x)^n$ – to include awareness of the range of values of x for which they are valid Derive the series expansions of simple compound functions Use of standard small angle approximations of sine, cosine and tangent
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¹ Unit 2A topic introduced at this stage to ensure all pre-requisite A2 Pure Maths is covered when teaching Further Maths in parallel. If not teaching in parallel, then this topic could be taught immediately after FM Unit 1 material.

² As above

Week	Teacher 1	Teacher 2
15		
16	Differential Equations <ul style="list-style-type: none"> • Use of integrating factor • General and particular solutions • Use of auxiliary equation to solve 2nd order homogeneous differential equations 	Centre of Mass <ul style="list-style-type: none"> • System of particles • Rods • Simple laminae • Composite laminae • Suspended laminae
17	<ul style="list-style-type: none"> • Solve 2nd order differential equations of the form $y'' + ay' + by = f(x)$, where $f(x)$, is <ul style="list-style-type: none"> ○ a polynomial function ○ an exponential function ○ a trigonometric function ○ not a solution of the corresponding homogeneous equation ○ Use the relationship between the case when the discriminant of the auxiliary equation is positive, zero and negative 	Frameworks <ul style="list-style-type: none"> • Light pin-jointed frameworks • Bow's notation optional • Thrusts/tensions
18	Damped Oscillations	
19	<ul style="list-style-type: none"> • Use of 2nd order differential equations 	Further Centre of Mass <ul style="list-style-type: none"> • Laminae and solids • Use of calculus • Composite bodies • Suspended bodies • Sliding/toppling
20	Force Systems	
21	<ul style="list-style-type: none"> • Resultant of a system of coplanar forces • Replace force system by <ul style="list-style-type: none"> ○ A single force 	
22	<ul style="list-style-type: none"> ○ A couple ○ A single force plus a couple 	Further Kinematics <ul style="list-style-type: none"> • Problems in 3 dimensions including use of calculus and vectors • Problems where acceleration is given as function of time, velocity or displacement • Examples involving constant power
23	Restitution	
24	<ul style="list-style-type: none"> • Problems involving <ul style="list-style-type: none"> ○ Smooth sphere ○ Smooth sphere and fixed plane 	

A2 Further Mathematics Units 1, 2A & 2C

Week	Teacher 1	Teacher 2
1	<p><u>Further Circular Motion</u>³</p> <ul style="list-style-type: none"> Banked corners Sliding Overturning (some introductory work on Moments will be required) 	<p><u>Polar Coordinates</u></p> <ul style="list-style-type: none"> Convert between polar and Cartesian coordinates Sketch curves with r given as function of θ Area enclosed by a polar curve
2		
3		
4	<p><u>Induction</u></p> <ul style="list-style-type: none"> Construction of proofs involving e.g. <ul style="list-style-type: none"> Sums of series Divisibility Powers of matrices 	<p><u>Complex numbers</u></p> <ul style="list-style-type: none"> Use of De Moivre's Theorem to find <ul style="list-style-type: none"> Multiple angle formulae Sums of series Use of <ul style="list-style-type: none"> $e^{i\theta} = \cos \theta + i \sin \theta$ $z = re^{i\theta}$ Find nth roots of $re^{i\theta}$ and relate to Argand diagram Use complex roots of unity to solve geometric problems
5		
6		
7	<p><u>Hyperbolic Functions</u></p> <ul style="list-style-type: none"> Definitions of $\sinh x$, $\cosh x$ and $\tanh x$, including domains, ranges and graphs Differentiate hyperbolic functions Integrate hyperbolic functions Definitions of inverse hyperbolic functions, including domains and ranges Derive and use the logarithmic forms of the inverse hyperbolic functions 	<p><u>Simple Harmonic Motion</u>⁴</p> <ul style="list-style-type: none"> Standard results Solution of SHM equation Simple pendulum Oscillations involving elastic strings
8		
9		
10	<p><u>Further Calculus</u></p> <ul style="list-style-type: none"> Evaluate improper integrals Integration using partial fractions – to include quadratic factors in denominator Differentiate inverse trig functions Integrate functions of the form $(a^2 - x^2)^{-1/2}$ and $(a^2 + x^2)^{-1}$ and choose the appropriate trigonometric substitutions to integrate associated functions Integrate functions of the form $(x^2 + a^2)^{-1/2}$ and $(x^2 - a^2)^{-1/2}$ and choose the appropriate hyperbolic substitutions to integrate associated functions Repeated integration by parts Reduction formulae 	<p><u>Series</u></p> <ul style="list-style-type: none"> Decompose rational functions into partial fractions – to include quadratic factors in denominator Use of formulae for sums of integers, squares and cubes to find sums of other series Use method of differenced for summation of series – to include use of partial fractions Find the Maclaurin series of a function – to include the general term Recognise and use the Maclaurin series for e^x, $\ln(1 + x)$, $\sin x$, $\cos x$ and $(1 + x)^n$ – to include awareness of the range of values of x for which they are valid Derive the series expansions of simple compound functions Use of standard small angle approximations of sine, cosine and tangent
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³ Unit 2A topic introduced at this stage to ensure all pre-requisite A2 Pure Maths is covered when teaching Further Maths in parallel. If not teaching in parallel, then this topic could be taught immediately after FM Unit 1 material.

⁴ As above

Week	Teacher 1	Teacher 2
15		
16	Differential Equations <ul style="list-style-type: none"> • Use of integrating factor • General and particular solutions • Use of auxiliary equation to solve 2nd order homogeneous differential equations 	Centre of Mass <ul style="list-style-type: none"> • System of particles • Rods • Simple laminae • Composite laminae • Suspended laminae
17	<ul style="list-style-type: none"> • Solve 2nd order differential equations of the form $y'' + ay' + by = f(x)$, where $f(x)$, is <ul style="list-style-type: none"> ○ a polynomial function ○ an exponential function ○ a trigonometric function ○ not a solution of the corresponding homogeneous equation ○ Use the relationship between the case when the discriminant of the auxiliary equation is positive, zero and negative 	Frameworks <ul style="list-style-type: none"> • Light pin-jointed frameworks • Bow's notation optional • Thrusts/tensions
18	Damped Oscillations	
19	<ul style="list-style-type: none"> • Use of 2nd order differential equations 	Linear Combinations <ul style="list-style-type: none"> • Use $E(aX + bY)$ and $Var(aX + bY)$ where X and Y are independent random variables • Solution of problems involving linear combinations of independent normally distributed variables
20	Sampling and Estimation	
21	<ul style="list-style-type: none"> • Use of Central Limit Theorem • Calculate point estimates of the population mean and variance • Use of standard error of the mean • Calculate confidence limits for the population mean 	
22	t - tests	χ^2 tests
23	<ul style="list-style-type: none"> • Understanding of when to use the t-distribution 	<ul style="list-style-type: none"> • Fit a theoretical distribution to given data
24	<ul style="list-style-type: none"> • Carry out a hypothesis test for the population mean • Formulate a hypothesis and carry out a two-sample or paired- sample t-test for the difference of the sample means 	<ul style="list-style-type: none"> • Use a χ^2 test with the appropriate number of degrees of freedom to carry out the corresponding goodness of fit test • Use a χ^2 test with the appropriate number of degrees of freedom to test for independence in a contingency table

A2 Further Mathematics Units 1, 2A & 2D

Week	Teacher 1	Teacher 2
1	<p>Further Circular Motion⁵</p> <ul style="list-style-type: none"> Banked corners Sliding Overturning (some introductory work on Moments will be required) 	<p>Polar Coordinates</p> <ul style="list-style-type: none"> Convert between polar and Cartesian coordinates Sketch curves with r given as function of θ Area enclosed by a polar curve
2		
3		
4	<p>Induction</p> <ul style="list-style-type: none"> Construction of proofs involving e.g. <ul style="list-style-type: none"> Sums of series Divisibility Powers of matrices 	<p>Complex numbers</p> <ul style="list-style-type: none"> Use of De Moivre's Theorem to find <ul style="list-style-type: none"> Multiple angle formulae Sums of series Use of <ul style="list-style-type: none"> $e^{i\theta} = \cos \theta + i \sin \theta$ $z = re^{i\theta}$ Find nth roots of $re^{i\theta}$ and relate to Argand diagram Use complex roots of unity to solve geometric problems
5		
6		
7	<p>Hyperbolic Functions</p> <ul style="list-style-type: none"> Definitions of $\sinh x$, $\cosh x$ and $\tanh x$, including domains, ranges and graphs Differentiate hyperbolic functions Integrate hyperbolic functions Definitions of inverse hyperbolic functions, including domains and ranges Derive and use the logarithmic forms of the inverse hyperbolic functions 	<p>Simple Harmonic Motion⁶</p> <ul style="list-style-type: none"> Standard results Solution of SHM equation Simple pendulum Oscillations involving elastic strings
8		
9		
10	<p>Further Calculus</p> <ul style="list-style-type: none"> Evaluate improper integrals Integration using partial fractions – to include quadratic factors in denominator Differentiate inverse trig functions Integrate functions of the form $(a^2 - x^2)^{-1/2}$ and $(a^2 + x^2)^{-1}$ and choose the appropriate trigonometric substitutions to integrate associated functions Integrate functions of the form $(x^2 + a^2)^{-1/2}$ and $(x^2 - a^2)^{-1/2}$ and choose the appropriate hyperbolic substitutions to integrate associated functions Repeated integration by parts Reduction formulae 	<p>Series</p> <ul style="list-style-type: none"> Decompose rational functions into partial fractions – to include quadratic factors in denominator Use of formulae for sums of integers, squares and cubes to find sums of other series Use method of differenced for summation of series – to include use of partial fractions Find the Maclaurin series of a function – to include the general term Recognise and use the Maclaurin series for e^x, $\ln(1 + x)$, $\sin x$, $\cos x$ and $(1 + x)^n$ – to include awareness of the range of values of x for which they are valid Derive the series expansions of simple compound functions Use of standard small angle approximations of sine, cosine and tangent
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13		
14		

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⁶ As above

Week	Teacher 1	Teacher 2
15		Centre of Mass
16	Differential Equations <ul style="list-style-type: none"> • Use of integrating factor • General and particular solutions • Use of auxiliary equation to solve 2nd order homogeneous differential equations 	<ul style="list-style-type: none"> • System of particles • Rods • Simple laminae • Composite laminae • Suspended laminae
17	<ul style="list-style-type: none"> • Solve 2nd order differential equations of the form $y'' + ay' + by = f(x)$, where $f(x)$, is <ul style="list-style-type: none"> ○ a polynomial function ○ an exponential function ○ a trigonometric function ○ not a solution of the corresponding homogeneous equation ○ Use the relationship between the case when the discriminant of the auxiliary equation is positive, zero and negative 	Frameworks <ul style="list-style-type: none"> • Light pin-jointed frameworks • Bow's notation optional • Thrusts/tensions
18	Damped Oscillations	
19	<ul style="list-style-type: none"> • Use of 2nd order differential equations 	Algorithms on Graphs
20	Graph Theory <ul style="list-style-type: none"> • Vertex and edge colouring 	<ul style="list-style-type: none"> • Nearest neighbour algorithm • Solution of problems using PERT • Two variable linear programming problems
21	<ul style="list-style-type: none"> • Cutsets and max-flow min-cut theorem • Bipartite graphs • Hall's marriage theorem 	Counting
22	Group Theory	<ul style="list-style-type: none"> • Principle of Inclusion and Exclusion • Derangements • Rook polynomials
23	<ul style="list-style-type: none"> • Symmetry groups – to include 	Generating Functions
24	<ul style="list-style-type: none"> ○ Cyclic group C_n ○ Dihedral group D_{2n} ○ Symmetry groups of the cube, octahedron and tetrahedron ○ Concept of cycle index ○ Use of table of cycle indices for simple symmetry groups ○ Polya's Enumeration Theorem ○ Use of the pattern inventory for 2 colours and the similar result for 3 colours 	<ul style="list-style-type: none"> • Understating of a generating function • Formulation of a generating function to solve simple summation problems • Use combinatorial arguments and elementary generating functions to prove simple formulae

A2 Further Mathematics Units 1, 2C & 2D

Week	Teacher 1	Teacher 2
1	<p><u>Group Theory</u>⁷</p> <ul style="list-style-type: none"> • Symmetry groups – to include <ul style="list-style-type: none"> ○ Cyclic group C_n ○ Dihedral group D_{2n} ○ Symmetry groups of the cube, octahedron and tetrahedron ○ Concept of cycle index ○ Use of table of cycle indices for simple symmetry groups ○ Polya's Enumeration Theorem • Use of the pattern inventory for 2 colours and the similar result for 3 colours 	<p><u>Polar Coordinates</u></p> <ul style="list-style-type: none"> • Convert between polar and Cartesian coordinates • Sketch curves with r given as function of θ • Area enclosed by a polar curve
2		<p><u>Complex numbers</u></p> <ul style="list-style-type: none"> • Use of De Moivre's Theorem to find <ul style="list-style-type: none"> ○ Multiple angle formulae ○ Sums of series • Use of <ul style="list-style-type: none"> ○ $e^{i\theta} = \cos \theta + i \sin \theta$ ○ $z = re^{i\theta}$ • Find nth roots of $re^{i\theta}$ and relate to Argand diagram • Use complex roots of unity to solve geometric problems
3		
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5	<p><u>Induction</u></p> <ul style="list-style-type: none"> • Construction of proofs involving e.g. <ul style="list-style-type: none"> ○ Sums of series ○ Divisibility ○ Powers of matrices 	<p><u>Graph Theory</u>⁸</p> <ul style="list-style-type: none"> • Vertex and edge colouring • Cutsets and max-flow min-cut theorem • Bipartite graphs • Hall's marriage theorem
6		
7		
8	<p><u>Hyperbolic Functions</u></p> <ul style="list-style-type: none"> • Definitions of $\sinh x$, $\cosh x$ and $\tanh x$, including domains, ranges and graphs • Differentiate hyperbolic functions • Integrate hyperbolic functions • Definitions of inverse hyperbolic functions, including domains and ranges • Derive and use the logarithmic forms of the inverse hyperbolic functions 	<p><u>Series</u></p> <ul style="list-style-type: none"> • Decompose rational functions into partial fractions – to include quadratic factors in denominator • Use of formulae for sums of integers, squares and cubes to find sums of other series • Use method of differenced for summation of series – to include use of partial fractions • Find the Maclaurin series of a function – to include the general term • Recognise and use the Maclaurin series for e^x, $\ln(1+x)$, $\sin x$, $\cos x$ and $(1+x)^n$ – to include awareness of the range of values of x for which they are valid • Derive the series expansions of simple compound functions • Use of standard small angle approximations of sine, cosine and tangent
9		
10	<p><u>Further Calculus</u></p> <ul style="list-style-type: none"> • Evaluate improper integrals • Integration using partial fractions – to include quadratic factors in denominator • Differentiate inverse trig functions • Integrate functions of the form $(a^2 - x^2)^{-1/2}$ and $(a^2 + x^2)^{-1}$ and choose the appropriate trigonometric substitutions to integrate associated functions • Integrate functions of the form $(x^2 + a^2)^{-1/2}$ and $(x^2 - a^2)^{-1/2}$ and choose the appropriate hyperbolic substitutions to integrate associated functions • Repeated integration by parts • Reduction formulae 	<p><u>Algorithms on Graphs</u></p> <ul style="list-style-type: none"> • Nearest neighbour algorithm • Solution of problems using PERT • Two variable linear programming problems
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⁷ Unit 2D topic introduced at this stage to ensure all pre-requisite A2 Pure Maths is covered when teaching Further Maths in parallel. If not teaching in parallel, then this topic could be taught immediately after FM Unit 1 material.

⁸ As above

Week	Teacher 1	Teacher 2
16	Differential Equations <ul style="list-style-type: none"> • Use of integrating factor • General and particular solutions • Use of auxiliary equation to solve 2nd order homogeneous differential equations • Solve 2nd order differential equations of the form $y'' + ay' + by = f(x)$, where $f(x)$, is <ul style="list-style-type: none"> ○ a polynomial function ○ an exponential function ○ a trigonometric function ○ not a solution of the corresponding homogeneous equation ○ Use the relationship between the case when the discriminant of the auxiliary equation is positive, zero and negative 	Counting <ul style="list-style-type: none"> • Principle of Inclusion and Exclusion • Derangements • Rook polynomials
17		
18	Linear Combinations <ul style="list-style-type: none"> • Use $E(aX + bY)$ and $\text{Var}(aX + bY)$ where X and Y are independent random variables • Solution of problems involving linear combinations of independent normally distributed variables 	Generating Functions <ul style="list-style-type: none"> • Understating of a generating function • Formulation of a generating function to solve simple summation problems • Use combinatorial arguments and elementary generating functions to prove simple formulae
19		
20	t – tests <ul style="list-style-type: none"> • Understanding of when to use the t-distribution • Carry out a hypothesis test for the population mean • Formulate a hypothesis and carry out a two-sample or paired- sample t-test for the difference of the sample means 	Sampling and Estimation <ul style="list-style-type: none"> • Use of Central Limit Theorem • Calculate point estimates of the population mean and variance • Use of standard error of the mean • Calculate confidence limits for the population mean
21		χ^2 tests <ul style="list-style-type: none"> • Fit a theoretical distribution to given data • Use a χ^2 test with the appropriate number of degrees of freedom to carry out the corresponding goodness of fit test • Use a χ^2 test with the appropriate number of degrees of freedom to test for independence in a contingency table
22		
23		
24		