



*Rewarding Learning*

**General Certificate of Secondary Education**

---

# **Mathematical Formulae and Tables**

---

For use by candidates taking examinations in  
GCSE Further Mathematics (Revised)

**For use from Summer 2019**

## **Appendix 1**

---

**BLANK PAGE**

<b>CONTENTS</b>	<b>Page(s)</b>
<b>Pure Mathematics Unit 1</b>	<b>1</b>
Formula Sheet	1
<b>Mechanics Unit 2</b>	<b>2</b>
Formula Sheet	2
<b>Statistics Unit 3</b>	<b>3</b>
Formula Sheet	3
<b>Statistical Tables Unit 3</b>	<b>4</b>
Normal Probability Table	4



## Formula Sheet

### PURE MATHEMATICS

Quadratic equations: If  $ax^2 + bx + c = 0$  ( $a \neq 0$ )

$$\text{then } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Differentiation: If  $y = ax^n$  then  $\frac{dy}{dx} = nax^{n-1}$

Integration:  $\int ax^n dx = \frac{ax^{n+1}}{n+1} + c$  ( $n \neq -1$ )

Logarithms: If  $a^x = n$  then  $x = \log_a n$

$$\log(ab) = \log a + \log b$$

$$\log\left(\frac{a}{b}\right) = \log a - \log b$$

$$\log a^n = n \log a$$

Matrices: If  $\mathbf{A} = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$   
then  $\det \mathbf{A} = ad - bc$

$$\text{and } \mathbf{A}^{-1} = \frac{1}{ad - bc} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix} \quad (ad - bc \neq 0)$$

## FORMULA SHEET

### MECHANICS

Quadratic equations: If  $ax^2 + bx + c = 0$  ( $a \neq 0$ )

$$\text{then } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Vectors: Magnitude of  $x\mathbf{i} + y\mathbf{j}$  is given by  $\sqrt{x^2 + y^2}$

Angle between  $x\mathbf{i} + y\mathbf{j}$  and  $\mathbf{i}$  is given by  $\tan^{-1}\left(\frac{y}{x}\right)$

Uniform Acceleration:  $v = u + at$   $s = \frac{1}{2}(u + v)t$   
 $v^2 = u^2 + 2as$   $s = ut + \frac{1}{2}at^2$

where  $u$  is initial velocity  $t$  is time  
 $v$  is final velocity  $s$  is change in displacement  
 $a$  is acceleration

Newton's Second Law:  $F = ma$

where  $F$  is resultant force  $m$  is mass  
 $a$  is acceleration

## FORMULA SHEET

### STATISTICS

Statistical measures: Mean =  $\frac{\Sigma fx}{\Sigma f}$

Standard deviation =  $\sqrt{\frac{\Sigma fx^2}{\Sigma f} - (\bar{x})^2}$

where  $\bar{x}$  is the mean

Probability:  $P(A \cup B) = P(A) + P(B) - P(A \cap B)$

$$P(A | B) = \frac{P(A \cap B)}{P(B)}$$

Bivariate Analysis: Spearman's coefficient of rank correlation is given by

$$r = 1 - \frac{6 \Sigma d^2}{n(n^2 - 1)}$$

NORMAL PROBABILITY TABLE

Table of  $\Phi(z)$

Z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990

